



**U.S. ARMY COMBAT CAPABILITIES
DEVELOPMENT COMMAND
ARMAMENTS CENTER**

**(U) IMPLEMENTATION OF IMPROVED METHODOLOGY
FOR HAZARDOUS FRAGMENT EVALUATION FOR BOTH
INSENSITIVE MUNITIONS & HAZARD CLASSIFICATION PURPOSES**

JANUARY 21-23, 2026

**(U) International Explosives Safety Summit
(IESSE)**

**(U) Phoenix Convention Center
Phoenix, Arizona, USA**

(U) Daniel J. Pudlak

FYSA – For those of you that did not attend my **previous talk**, I presented the **corrections** and **improvements** that we've made to the **metrics** governing the **Hazardous Fragment Curves** that the IM & HC communities use to evaluate fragment severity / hazardousness (**8J, 20J, 79J**), to serve preface this presentation in which we will discuss the new / proposed methodology for evaluating hazardous fragments during **IM & HC testing**.

- ❖ **'Improved Metrics'** discussed in this paper have been adopted by the NATO / IM communities via AOP-39.
 - Intention - familiarize / inform the HC / Safety community(ies) with:
 - ✓ Corrections we've made to the math behind the 8J, 20J & 79J curves that we all use
 - ✓ Improvements we've made to math behind the 8J, 20J & 79J curves that we all use
 - ✓ Additional New Curves that we've incorporated to take into account modern-day armament material.

- ❖ **'Improved Methodology'** paper (following presentation) discusses the new / proposed 'Energy-Density' methodology.
 - Brings forth a more scientifically accurate method of evaluating the severity / hazardousness of fragments, rather than the 'Energy' methodology that we all currently use.
 - This has not yet been adopted by the IM community, but...
 - Purpose is to solicit help to finalize the methodology for incorporation into the IM & HC / Safety evaluation processes.

recap...if needed.

Per MIL-STD-2105D / AOP-39(3):

- “At least **one piece** (e.g. casing, packaging, or energetic material) **travels** (or would have been capable of travelling) **beyond 15m and with an energy level greater than 20J** based on the distance versus mass relationships in figure 1.”
 - Where did 20J come from?
 - Why did we switch from 79J to 20J?
 - Why is 15m (50ft) significant?
 - Are these the best metrics?
 - What method are we using to measure these metrics?
 - Is there a better method to measure these metrics?

*Note:

- 79J in AOP-39 Ed 2 (2009) and MIL-STD-2105C (July 2003)
- 20J in AOP-39 Ed 3 (March 2010) and MIL-STD-2105D (April 2011)

Colonel Journee, French infantry officer established 15ft-lb & 58 ft-lb criterion in 1800's

- “Considered the **upper and lower bounds of what a man could endure** from recoil of a rifle”.
 - **15 ft-lb (20J)** was set as the **maximum recoil suitable for a military rifle**
 - **58 ft-lb (79J)** recoil energy was estimated to provide **significant bruising/damage to typical shoulder**

TOP 3-2-504 – Daily Firing limit for safety of hand and shoulder weapons

Weapon System	Muzzle Recoil Energy (ft-lbs)
Lee-Enfield Rifle	12.75 ft-lbs
.45 Cal. Rifle	14.40 ft-lbs
.30 Cal Garand	15.18 ft-lbs
Springfield '03 Rifle	14.98 ft-lbs

Computed Recoil Energy	Limitation
Less than 15 ft-lb (20.3 Joules)	Unlimited Firing
15-30 ft-lb (20.3 – 40.7 Joules)	200 rounds / day / shooter
30-45 ft-lb (40.7 – 61.0 Joules)	100 rounds / day / shooter
45-60 ft-lb (61.0 – 81.4 Joules)	25 rounds / day / shooter
Greater than 60 ft-lbs (81.4 Joules)	No Shoulder Firing

}
15 ft-lbs (20J) →

58 ft-lbs (79J) →

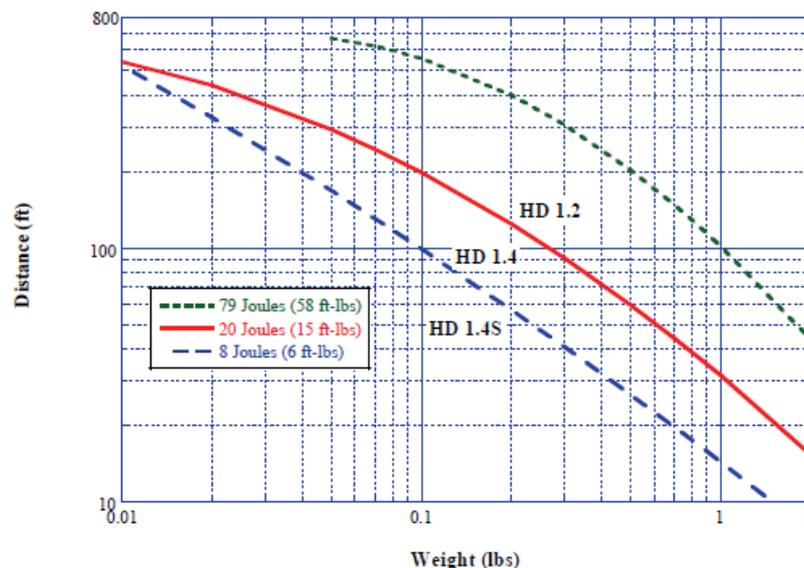
- » Shotguns produce 25 ft-lb to 35 ft-lb of recoil
- » Elephant gun produces ~ 52 ft-lb of recoil

“The recoil energy of the Lee-Enfield rifle is well below the maximum energy of recoil advisable for a military rifle, which should not exceed 15 foot pounds.” --1909 British Textbook of Small Arms

- Since then, 20J & 79J have been referenced and used for numerous applications
 - Testing standards, injury thresholds, toy/weapon limits, etc.
- Currently we use the fragment's mass and distance to calculate its energy.
 - Found that many projectiles are not lethal, or even very hazardous with 20J/79J.
- Examples of projectiles and their associated energy:
 - Paintball 300ft/s – **12J**
 - 0.177 cal pellet (air gun) 900ft/s– **21J**
 - Baseball 90mph – **120J**
 - 40mm non-lethal grenade 200ft/s – **150J**



Where did our 20J & 79J curves come from?

 TB 700-2
 NAVSEAINST 8020.8C/TO 11A-1-47

58 ft-lbs (79 J)

D in ft, M in lbs

$$D = 101.65 * M^{[-1.1061 - 0.15961 * \ln(M)]}$$

$$M = 4.24 * D^{[1.8714 - 1.2433 * (\ln(D)) + 0.25442 * (\ln(D))^2 - 0.018948 * (\ln(D))^3]}$$

D in m, M in kg

$$D = 11.697 * M^{[-1.35846 - 0.15961 * \ln(M)]}$$

$$M = 4.533 * D^{[0.132633 - 0.49695 * (\ln(D)) + 0.16437 * (\ln(D))^2 - 0.018948 * (\ln(D))^3]}$$

15 ft-lb (20 J)

D in ft, M in lbs

$$D = 31.49 * M^{[-0.98 - 0.0788 * \ln(M)]}$$

$$M = 0.000006151 * D^{[14.8843 - 6.0304 * (\ln(D)) + 1.0077 * (\ln(D))^2 - 0.06313 * (\ln(D))^3]}$$

D in m, M in kg

$$D = 4.212 * M^{[-1.103 - 0.0788 * \ln(M)]}$$

$$M = 0.1283 * D^{[4.399 - 2.973 * (\ln(D)) + 0.7077 * (\ln(D))^2 - 0.06313 * (\ln(D))^3]}$$

6 ft-lb (8 J)

D in ft, M in lbs

$$D = 14.41 * M^{[-0.896 - 0.0252 * \ln(M)]}$$

$$M = 7.2157 * D^{[0.6007 - 0.9509 * (\ln(D)) + 0.2155 * (\ln(D))^2 - 0.01758 * (\ln(D))^3]}$$

D in m, M in kg

$$D = 2.13 * M^{[-0.935 - 0.0252 * \ln(M)]}$$

$$M = 2.4193 * D^{[-0.8642 - 0.3317 * (\ln(D)) + 0.1319 * (\ln(D))^2 - 0.01758 * (\ln(D))^3]}$$

Figure 5-17
Relationship of Projection Kinetic Energy and Hazard Division

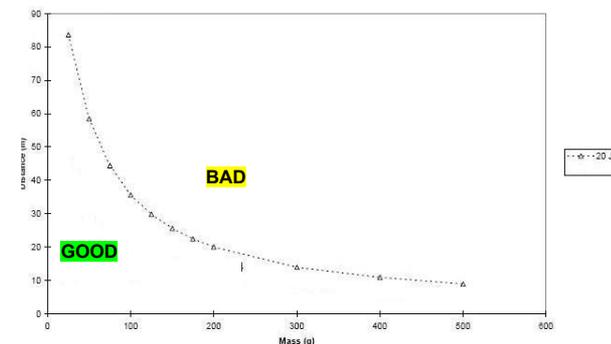
- Current Metric:

- $E_{\text{Fragment}} > 20\text{J}$ beyond 15m → TYPE IV
- $E_{\text{Fragment}} < 20\text{J}$ beyond 15m → TYPE V

- Current Method

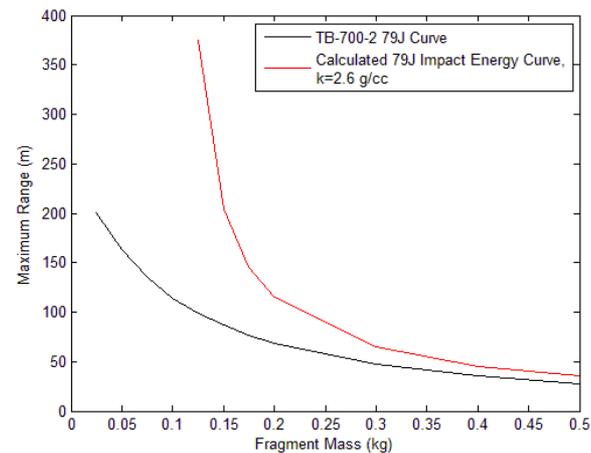
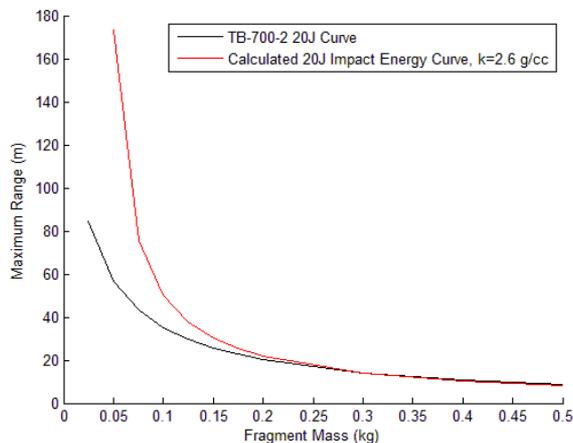
- Measurement of fragment location, orientation, weight, and condition.
- **Mass and Distance** are then used to determine if fragment energy was over 20J.
 - *Handy frag energy calculator
- If the fragment's energy is:
 - above the curve, TYPE IV
 - below the curve, TYPE V

Mass (g)	Projection distance (m)	
	20 J	8 J
25	83.6	46.8
50	58.4	28.7
75	44.4	20.6
100	35.6	16.2
125	29.8	13.3
150	25.6	11.4
175	22.43	10
200	20	8.8
300	13.9	6.3
400	10.9	4.9
500	8.9	4.1



Problem #1:

- **Current curve** we use was formulated with a **Launch Energy Criterion**
 - Works based on:
 - **Calculating the max distance a given mass can travel when launched with 20J.**
 - However, AOP-39 guidance indicates we should be measuring **Impact Energy.**
- **Solution #1:**
 - We reformulated both curves under consideration (20J & 79J) **based on **Impact Energy Criterion****

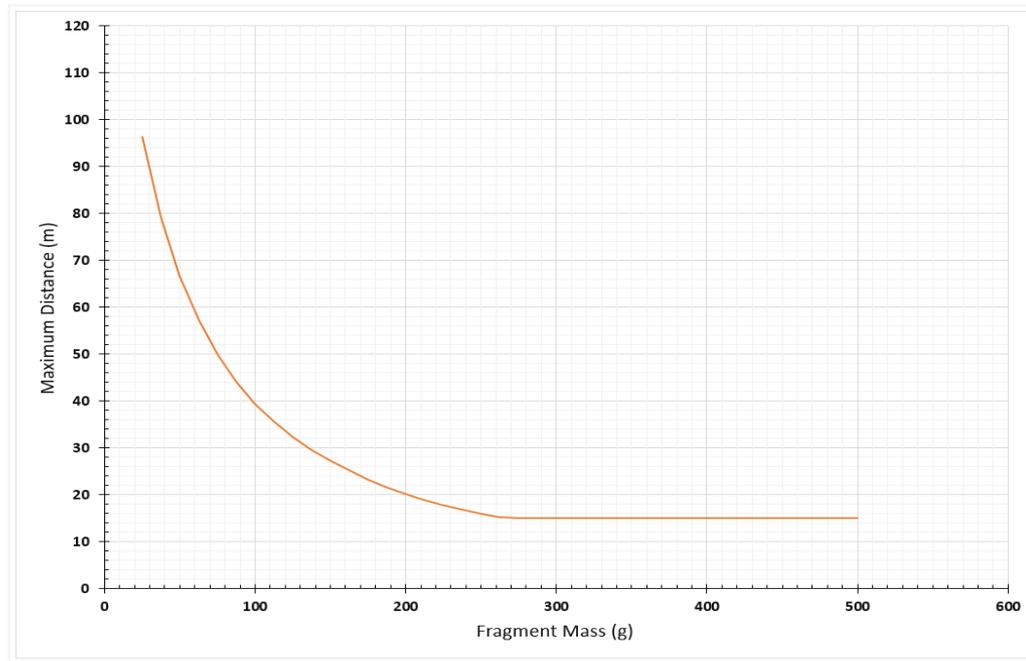


Problem #2:

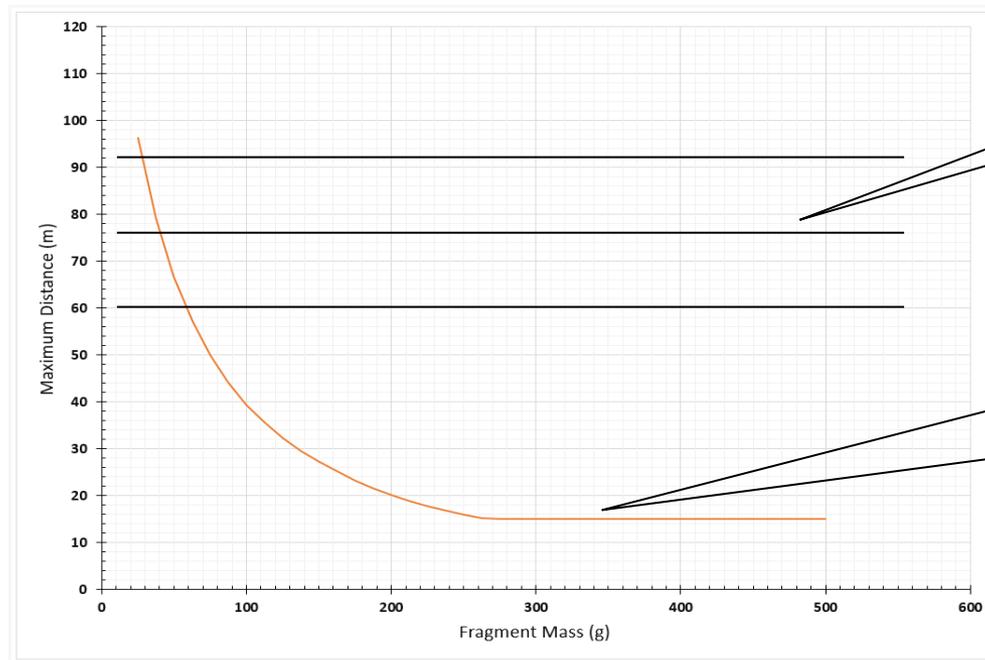
- Current curve doesn't take into account 15m.

• Solution #2:

- Incorporated 15m in 20J Impact Energy @ 15m curve.



- Curve still may not converge enough for Type IV/V fragments
 - Further investigation required to bound upper/lower limits



Arbitrary lines represent potential 'ceiling' for non-Type IV/V frags

Flattens out due to masses so large that cannot impact with at least 20J by virtue of its mass.

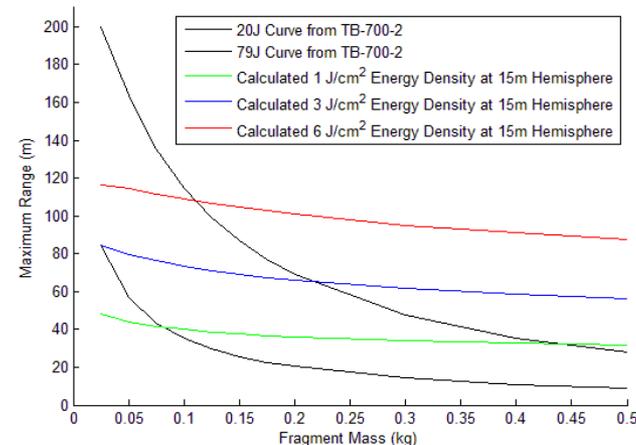
Does that resolve all issues?

Problem #3

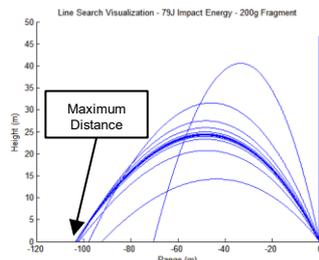
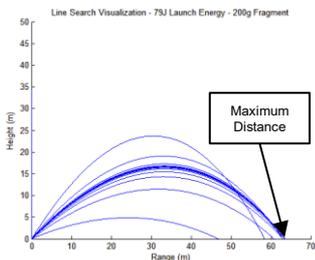
- Energy (J) alone is not a good measure of impact
 - Does not take into account the energy applied per the presented area
- Energy Density (J/cm^2) is a better measure of impact
 - Does take into account the energy applied per the presented area
- Example:
 - 32g, 2" diameter, object fired at 150fps produces 33.4J
 - 3.5g, 2" diameter, object fired at 230fps produces 8J
 - Both objects produce $\sim 3.8J/cm^2$
 - The key attribute is the presented area of the objects

Solution:

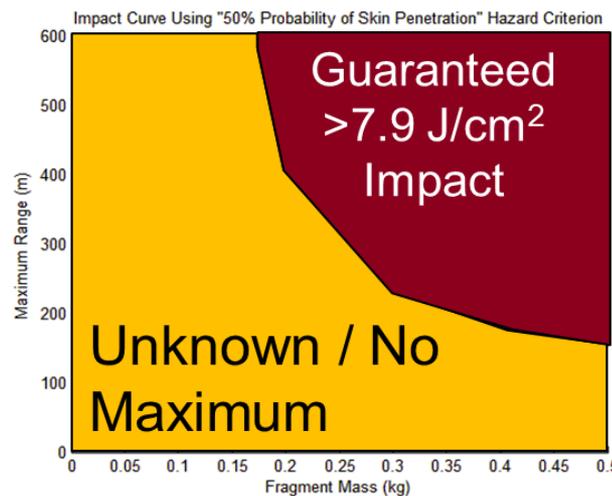
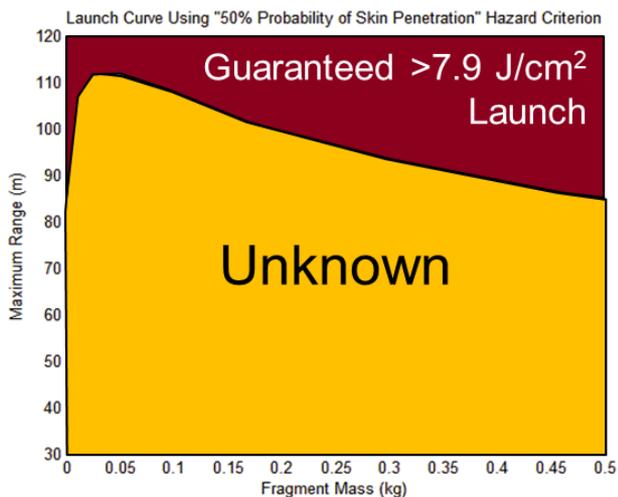
- ARDEC formulated Energy Density curves for
 - $1 J/cm^2$,
 - $3 J/cm^2$
 - $6 J/cm^2$



How does Energy Density Work?



- Energy Density can be used with either the:
 - Launch Energy Criterion or
 - Impact Energy Criterion
- Major difference is that mass is computed as a function of presented area:
 - $mass = k * (presented\ area)^{3/2}$
 - $k = 2600\ kg/m^3$
- The issue with using $7.9\ J/cm^2$, which is the 50% skin penetration model, distances are too large for IM purposes.



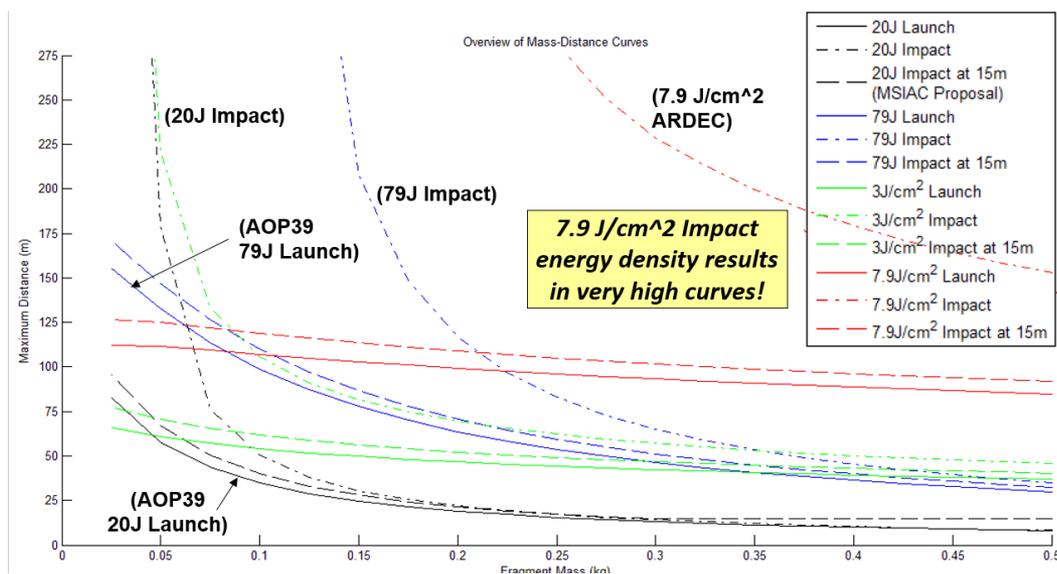
What is the solution?

Problem #4:

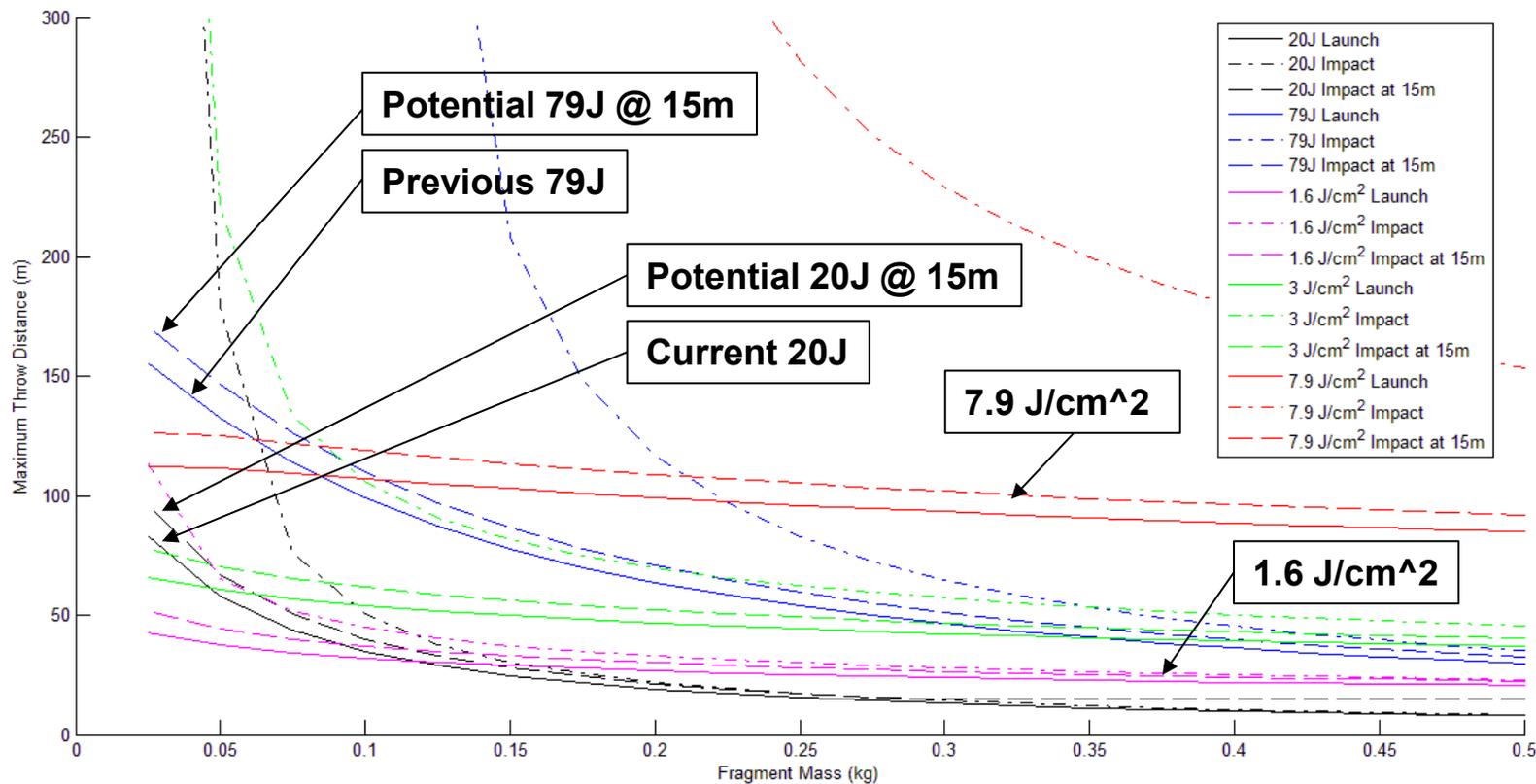
- What is an **acceptable metric** for using the **Energy Density Criterion**?
- What is an appropriate metric to use as threshold for hazardous fragment in the realm of IM Type IV/V fragments?

Solution #4:

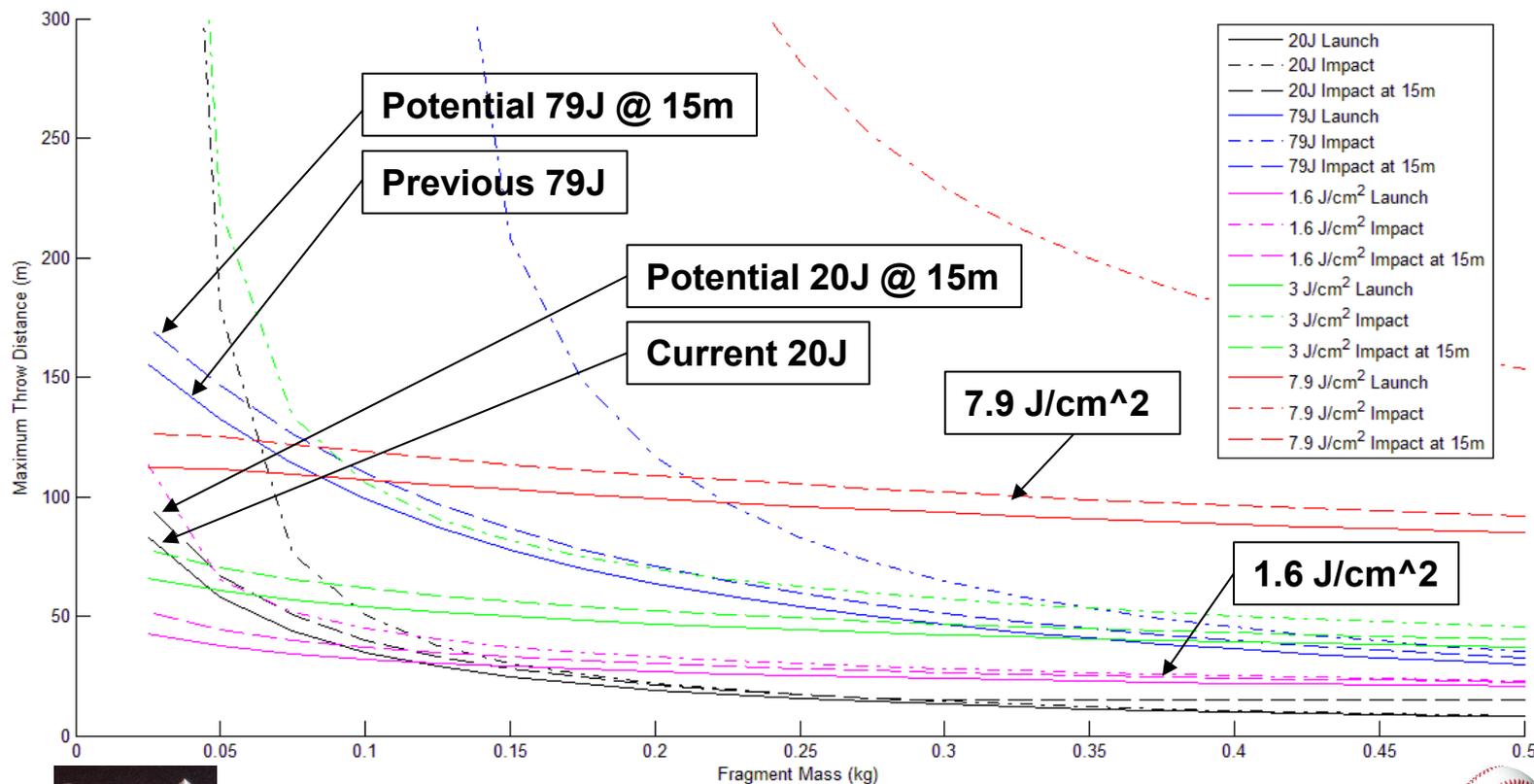
- Lethality & safety experts suggest **7.9 J/cm²** is more relevant to **penetration injury/impacts**.
- Literature research suggests **1.6 J/cm²** appropriate for human injury based on “**Blunt Theory**”.



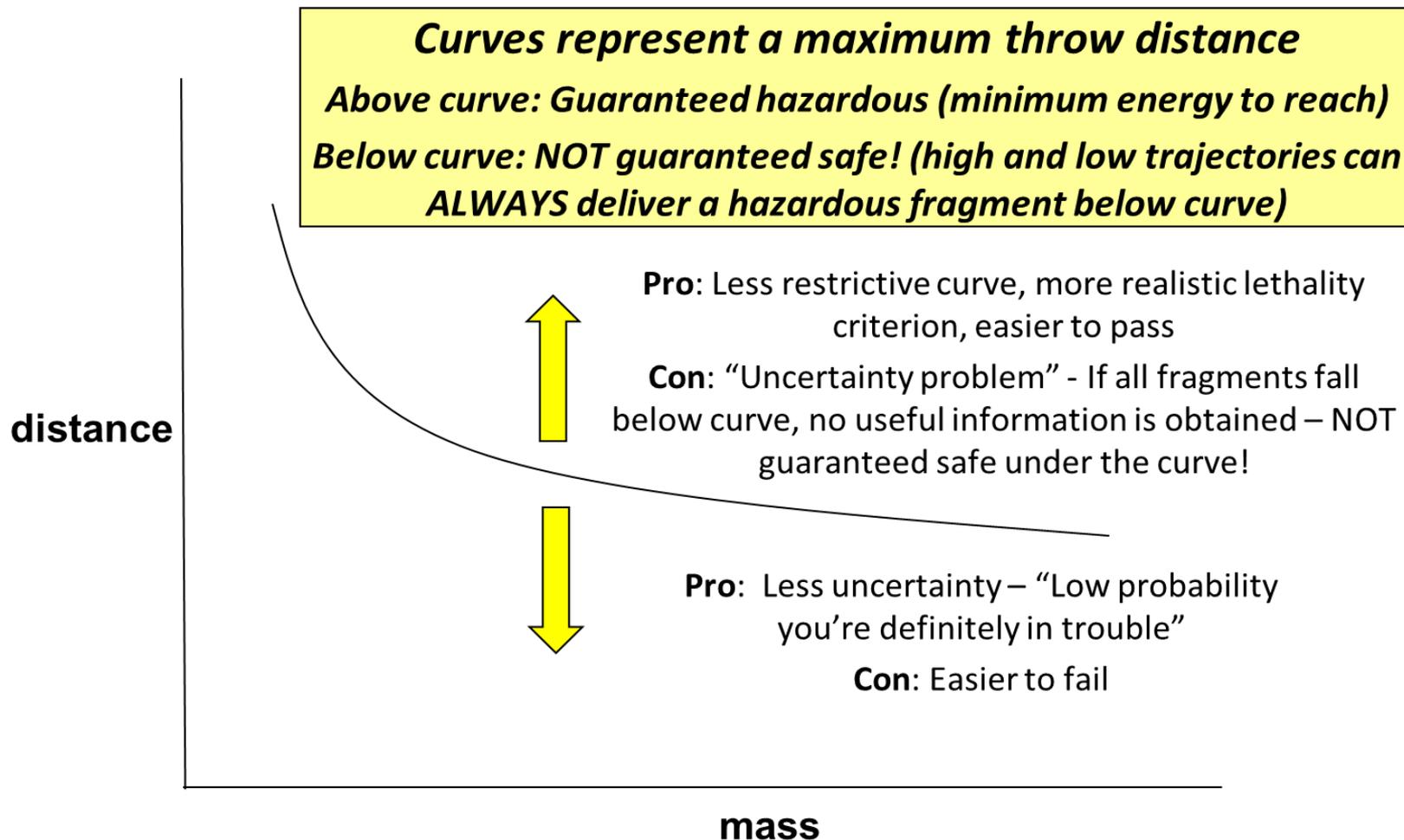
Comparison of Candidate Solutions



Comparison of Candidate Solutions



- Impact energy curves go off to infinity for small mass (terminal velocity)
 - Impact energy at 15m curves are very close to launch energy curves

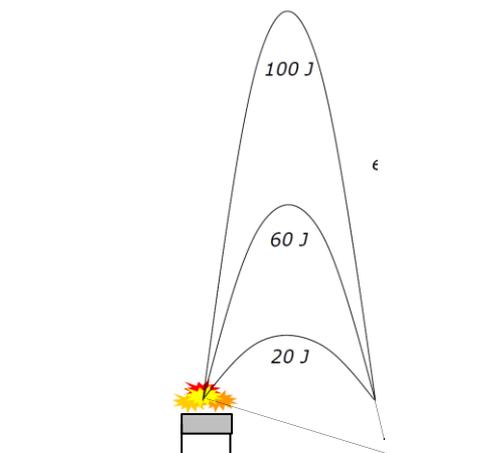
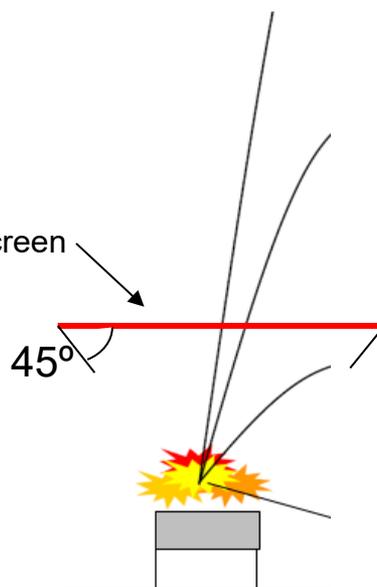


Risk: Frags under curve may have extremely high/low trajectories and may have travelled with high velocity/energy

Mitigation:

- Accept – We currently accept this risk
- Confirm trajectories utilizing equipment
 - HC witness screens
 - Cameras
 - Etc.

Example: HC Witness Screen

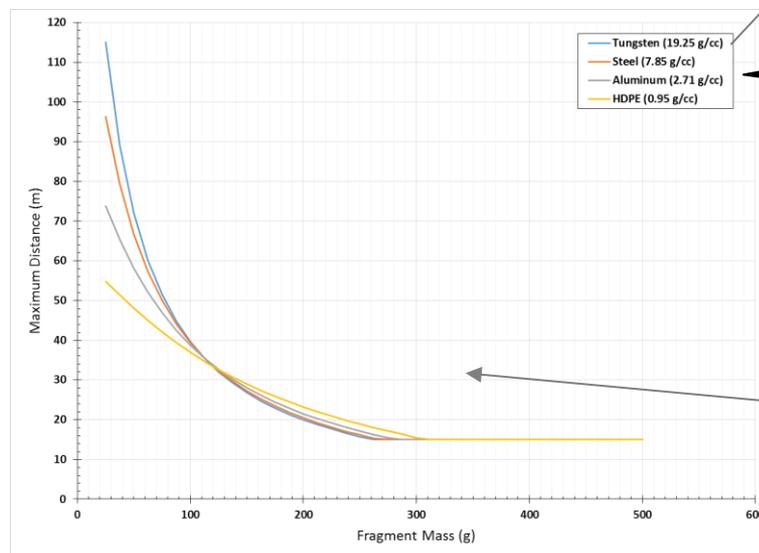


- Current curves assume chunky, tumbling, steel fragment
 - Not accurate evaluation for characteristic-unique fragments
 - Must consider other factors:
 - Density
 - Shape
 - Stability
 - Etc.
- Should be several curves to reference when evaluating unique fragment
- A set curves superimposed on one graph, each incorporating density, shape, and stability. User references specific curve for unique fragment.

For example: Density

- For fragments of different density than steel, effect of drag can be taken into account using the previous methodology.
 - Can group into four categories:
 - $\frac{3}{4}$ density of steel
 - $\frac{1}{2}$ density of steel
 - $\frac{1}{4}$ density of steel

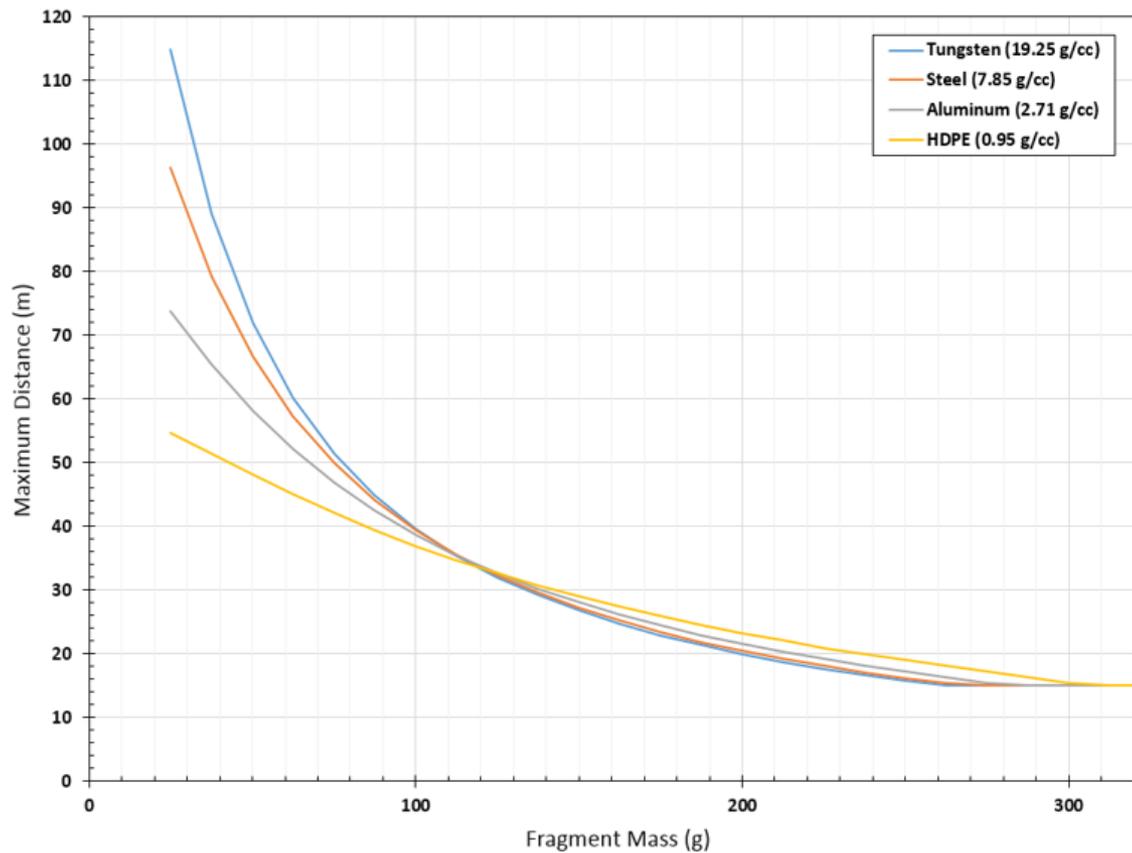
$$V = V_0 \exp\left(-\frac{\rho_{air} S C_D}{2m} x\right) = \sqrt{\frac{2E_0}{m}} \exp\left(-\frac{\rho_{air} \frac{3}{2} \left(\frac{m}{\rho_{frag}}\right)^{2/3} C_D}{2m} x\right)$$



For better accuracy, we implemented 4 new curves, 3 incorporating different densities of common armament materiel.

*Curves provided to NATO IM Working Group for inclusion into revised AOP-39

- This is what we implemented.



Implementation of Energy-Density Curves

Energy Density Methodology

- In order to implement, certain factors must be either known, calculated, or assumed.
 - *E.g. Impacting Surface Area of Fragment* must be accurately measured/assumed
 - Not easy for asymmetric fragments

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 - Some methods proposed:
 - Automated 3-D optical measurement device: ‘Icosahedron’
 - Generic fractional volume categories (“Frag-in-a-Box”)

Implementation of Energy-Density Curves

Energy Density Methodology

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- Some methods proposed:

- Automated 3-D optical measurement device: ‘Icosahedron’

- Generic fractional volume categories (“Frag-in-a-Box”)

- Cubical fragment

- » Cube occupies 4/4 of a cube’s volume



- Convex fragment

- » Sphere ~3/4 of the cube’s volume



- Concave fragment

- » Hour glass ~2/4 of the cube’s volume.



- Length/Diameter

- » Long, thin rod/strip ~1/4 of the cube’s volume.



- **Technically identify and justify Energy Density Methodology**

- Leverage with SMEs

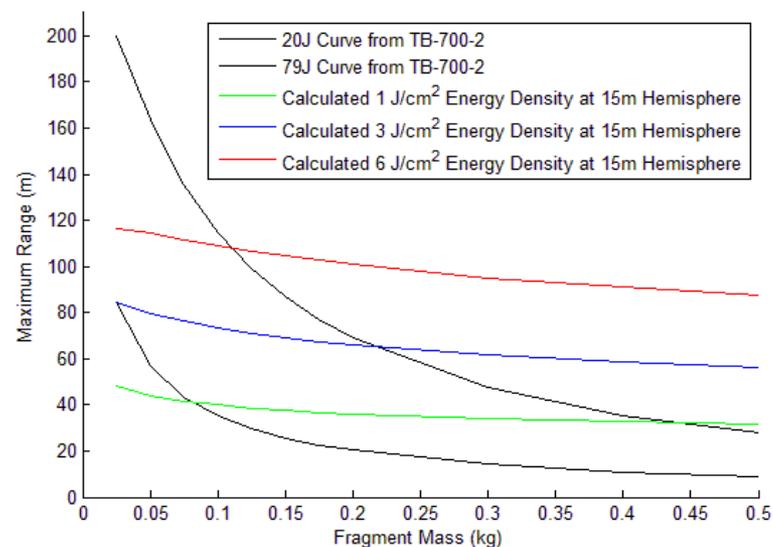
- ARDEC

- Aero ballisticians
- Lethality Division
- Non-Lethality Division
- System Effectiveness
- Biomedical Engineering

- TBRL

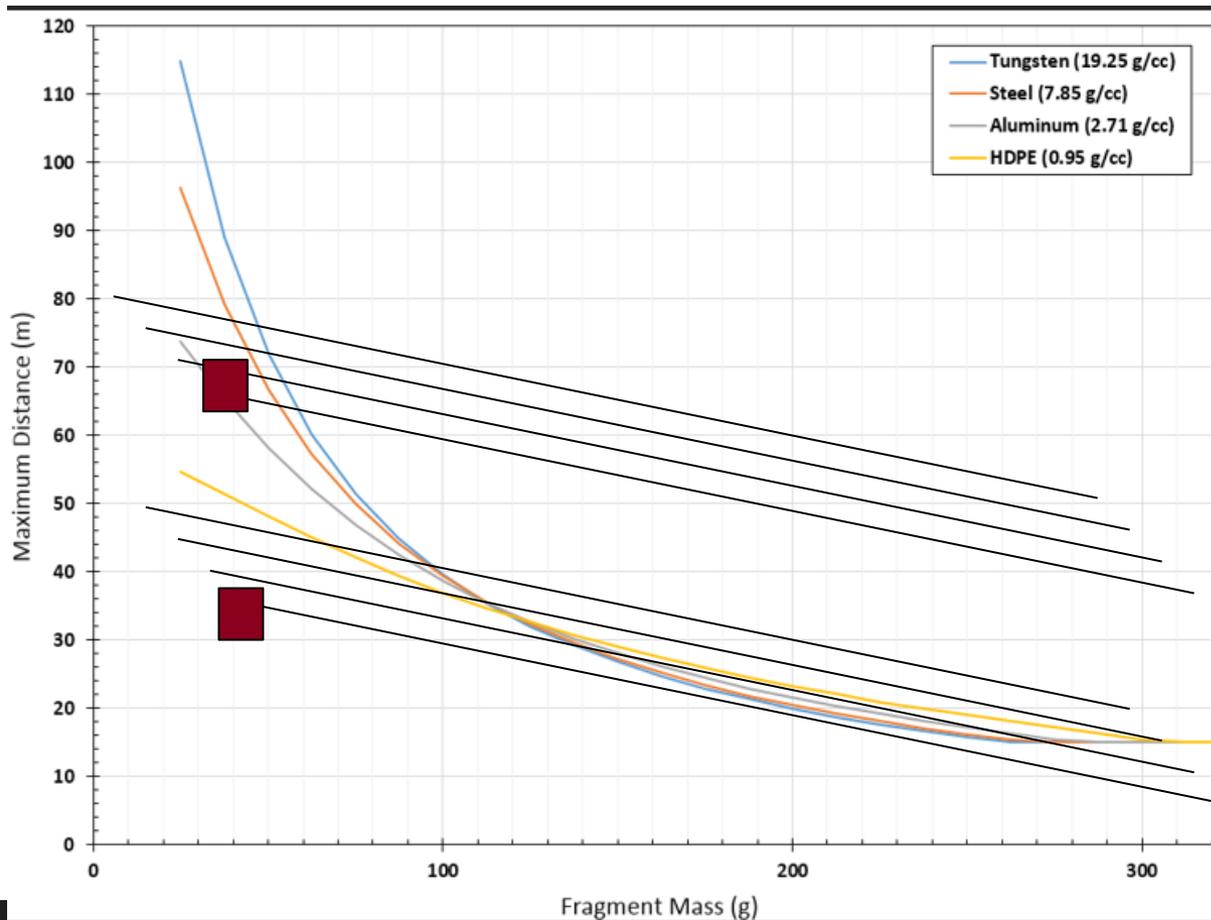
- ARL

- SLAAD



- Inherent issue with Mass-Distance curve for Pass/Fail Criteria
- Best we can do is fix current curve, and improve criteria
- ARDEC reformulated the curve with Impact Energy Criterion
- MSIAC reformulated Impact Energy Criterion @ 15m
 - Much more conservative approach than previous curve
- New / Fixed curves adopted by IM community → Suggest HC follow-suite
- The 20J vs 79J argument is irrelevant
 - Energy Density is better method to measure impacts/injury than energy alone
 - Literature and Lethality Experts suggest 1.6 J/cm² for our IM realm of Type IV/V fragments / injuries
 - Still needs work before implementation
 - NATO Response Descriptor Working Group (RDWG) Decision for incorporation into IM.

- This is all you need, however.



Questions?

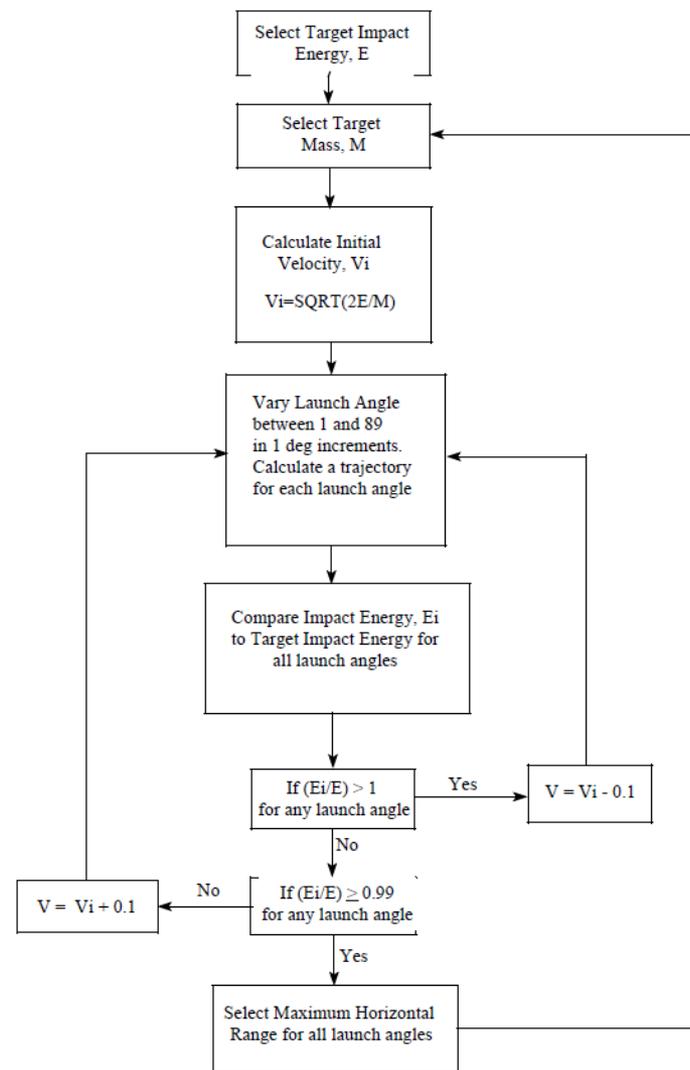


Back-up Slides



- What are we currently doing?
 - “Type IV (Deflagration)” if fragments found further than TB-700-2 20J curve
 - We spoke to the originators of the TB-700-2 curves, were provided with the following methodology
 - See flow chart they provided
 - Limits the maximum impact energy to 20J
 - The maximum impact energy *is* the launch energy (unless item is on a stand)
 - “at 15m” caveat not considered in their calculation
 - The TB-700-2 20J curve definitely represents maximum distance a fragment could be thrown at 20J launch energy

The 20J and 79J curves in both TB-700-2 and the UN Orange Book represent launch energy as a result of a mistake in the calculations





Equations of Motion (Vector Form)

$$\frac{d\mathbf{V}}{dt} = -\frac{\rho S C_D}{2m} |\mathbf{V}| \mathbf{V} + \mathbf{g}$$

$$\frac{d\mathbf{x}}{dt} = \mathbf{V}$$

F=ma with air drag

Equations of Motion (Scalar Form)

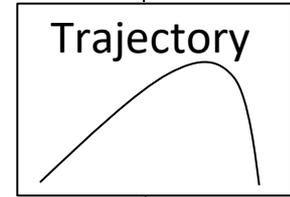
$$\frac{dV_x}{dt} = -\frac{\rho S C_D}{2m} V V_x = -\frac{\rho S C_D}{2m} V_x \sqrt{V_x^2 + V_y^2}$$

$$\frac{dV_y}{dt} = -\frac{\rho S C_D}{2m} V V_y - g = -\frac{\rho S C_D}{2m} V_y \sqrt{V_x^2 + V_y^2} - g$$

$$\frac{dx}{dt} = V_x$$

$$\frac{dy}{dt} = V_y$$

Curve Generation / Other Analysis



(Modeling approximations)

Shape factor data

$$m = kS^{3/2}$$

If the fragments from a given weapon are assumed to be geometrically similar, the mass m and presented area A are related by $m = kA^{3/2}$. Values of k , called a shape factor or ballistic density, may be determined from weight and presented area measurements on fragments recovered from tests of particular weapons. Although the value of k differs from one weapon to another, for forged steel projectiles and fragmentation bombs the average value of 660 grains/in.³ (2.60 g/cm³) has been recommended, while for demolition bombs the value 590 grains/in.³ (2.33 g/cm³) has been applied.

(from Zaker, DDESB-TP-12)

(2.60 g/cm³)

Drag Coefficient Data

TABLE I DRAG COEFFICIENTS FOR IRREGULAR FRAGMENTS

MACH NUMBER	DRAG COEFFICIENT
0	0.80
0.75	0.88
0.90	1.09
1.15	1.26
2.00	1.14
4.00	1.08
>4.00	1.08

Note: Drag coefficient varies linearly between Mach Number entries

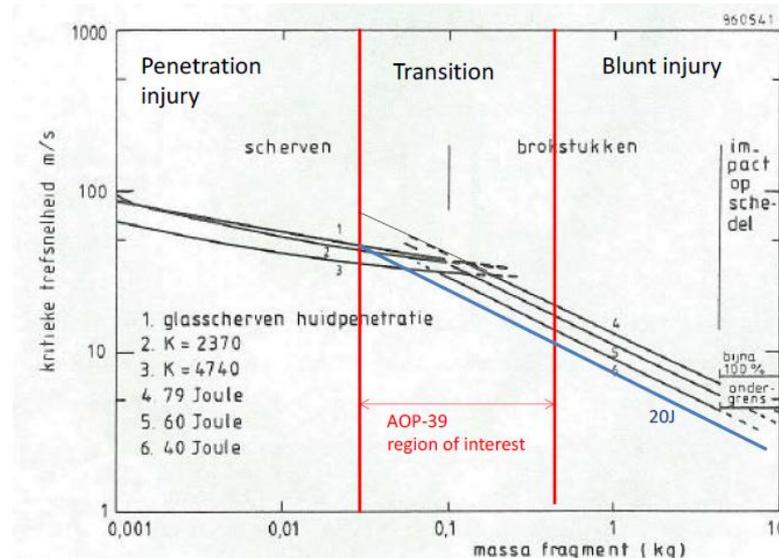
In Design Considerations for Toxic Chemical and Explosives Facilities; Scott, Ralph A., et al.; ACS Symposium Series; American Chemical Society: Washington, DC, 1987.

(from Swisdak, "Fragmentation Effects: An Overview")

- Numerical Solver**
- MATLAB ode45 (variable-timestep Runge-Kutta)
 - Validate with flat fire solutions / ensure same results obtained for very small constant timestep
 - Can run backwards or forwards in time
 - Launch height usually zero
 - Stop integration when trajectory ordinate becomes negative

Ballistic trajectory calculations like these are where the TB-700-2 curves came from

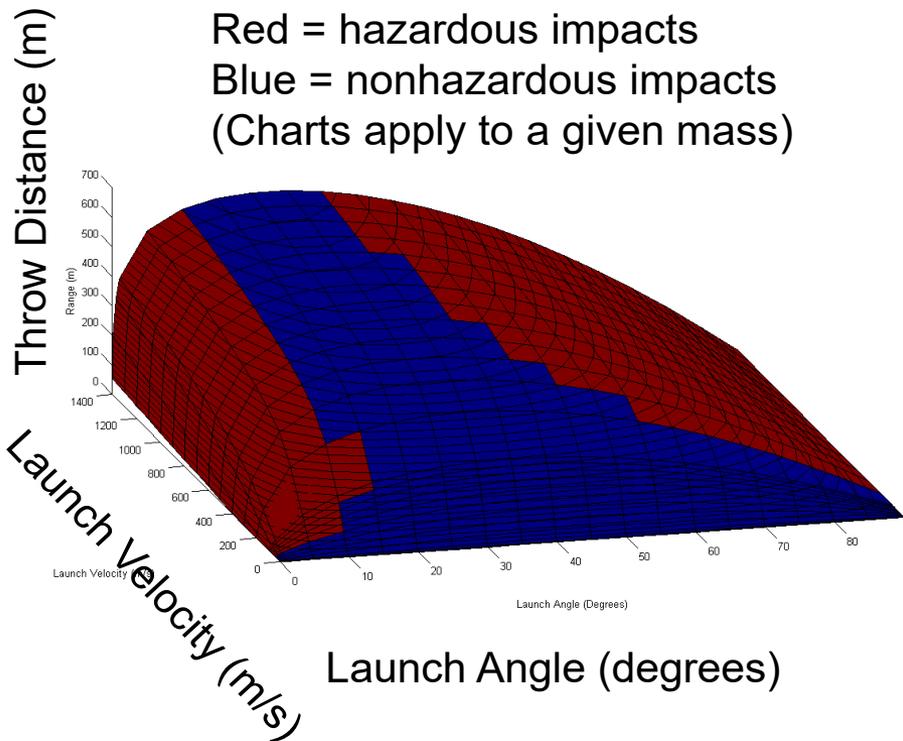
- According to MSIAC:
 - Energy/Area more relevant for skin penetration
 - Energy more relevant for blunt trauma
 - Fragments in region of interest are big enough to start causing blunt trauma injuries at relatively low velocities
 - Furthermore, blunt trauma injuries will be caused at lower velocities thus a skin penetration criterion is not conservative
- It is conceivable that steel fragments of the sizes in AOP-39 can be thought of as relatively dangerous at relatively slow speeds
- Intuitive considerations regarding absorption of the impact energy
 - Partitioning of impact energy between projectile and target (energy absorbing structural deformation)
 - Distribution of force over impact surface
- US lethality experts should be consulted on what criterion makes sense for the fragments in this



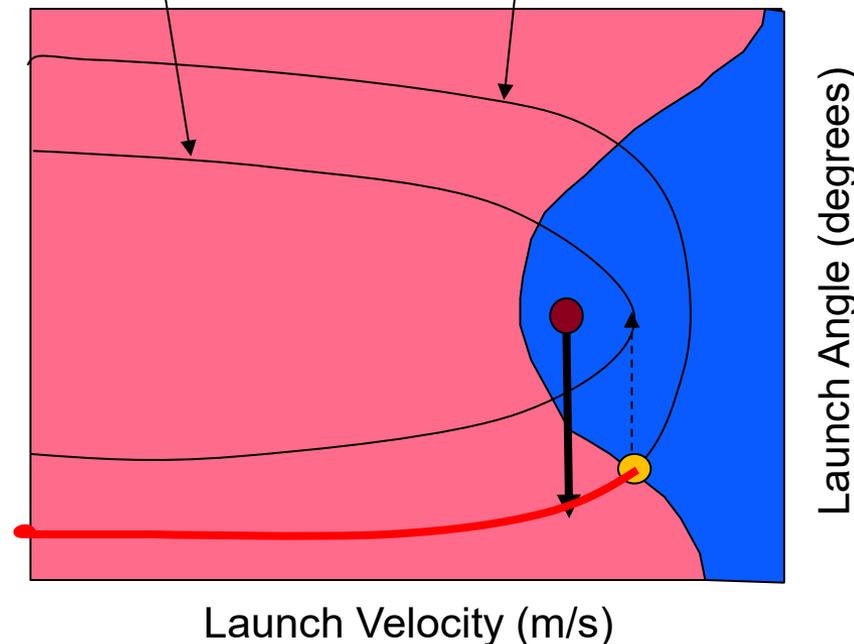
From Martijn van der Voort, "ANALYSIS OF THE IM TYPE V RESPONSE DESCRIPTOR"

Impact Energy at 15m (MSIAC Proposal) (Cont'd)

Red = hazardous impacts
Blue = nonhazardous impacts
(Charts apply to a given mass)



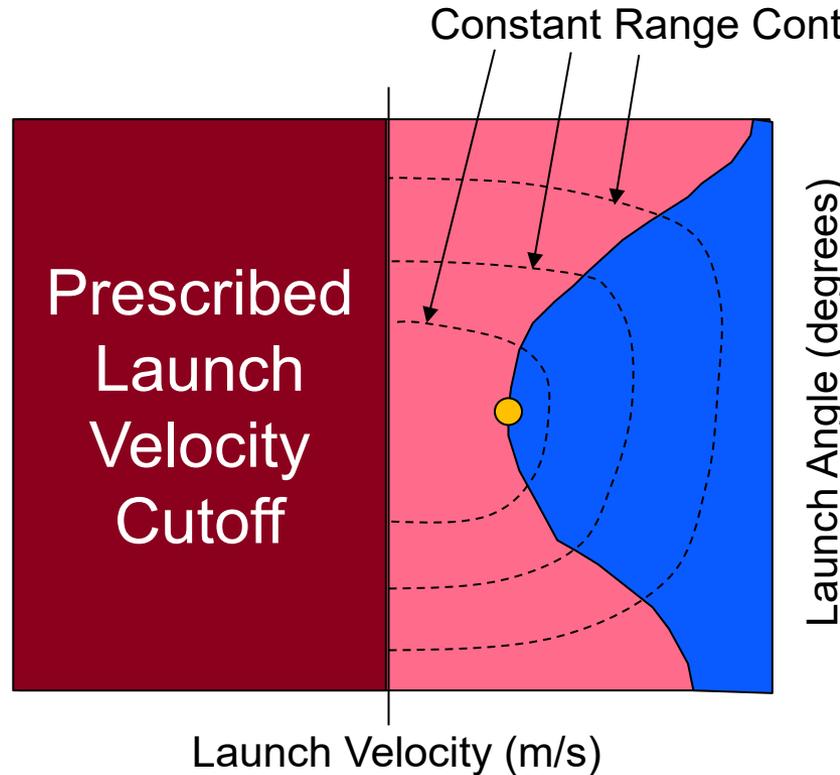
Range > 15m contour (point on the mass-distance curve)
Range=15m contour



Fragments which land above MSIAC curve are guaranteed to hit 15m with a hazardous fragment if the launch angle were lowered

- Minimum velocity for hazardous impact at 15m
- Fragment found above MSIAC proposed curve
- Hazardous Impacts

Uncertainty Reduction Strategies - Probability Methodology



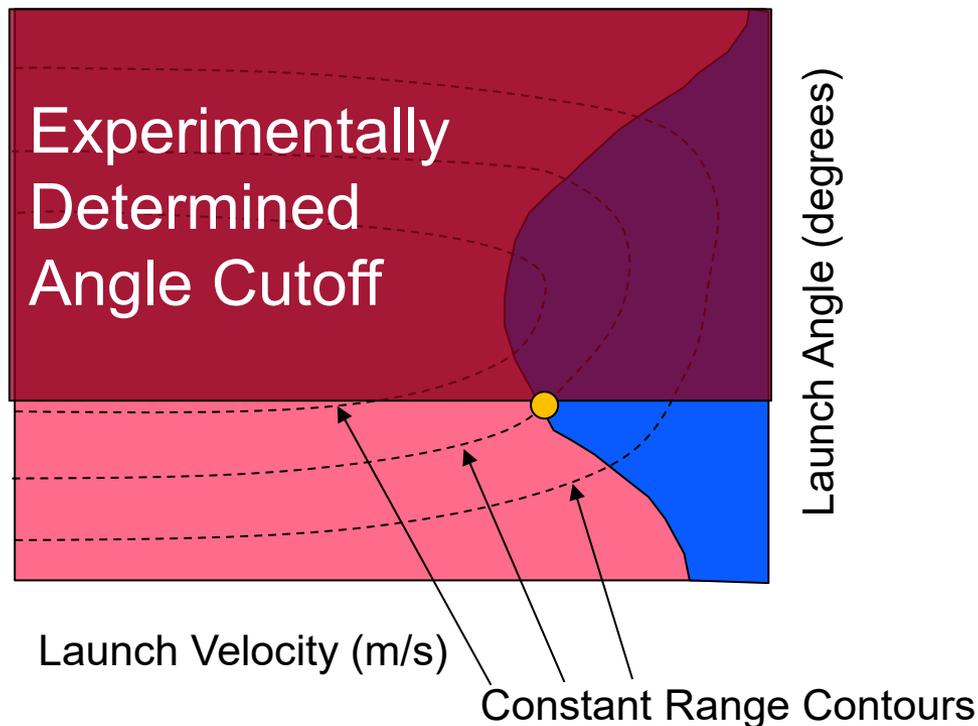
Fragments just under the curve have a (quantifiable) higher probability of being hazardous than fragments further below the curve

-  Point used for impact mass-distance curve
-  Impacts Not Considered
-  Hazardous Impacts

Probability that a fragment under the curve is hazardous can be computed (~ratio of areas) if a launch velocity cutoff is prescribed and all trajectories equally likely

Hazardous Impacts

Uncertainty Reduction Strategies - Angle Cutoffs (Experimental)



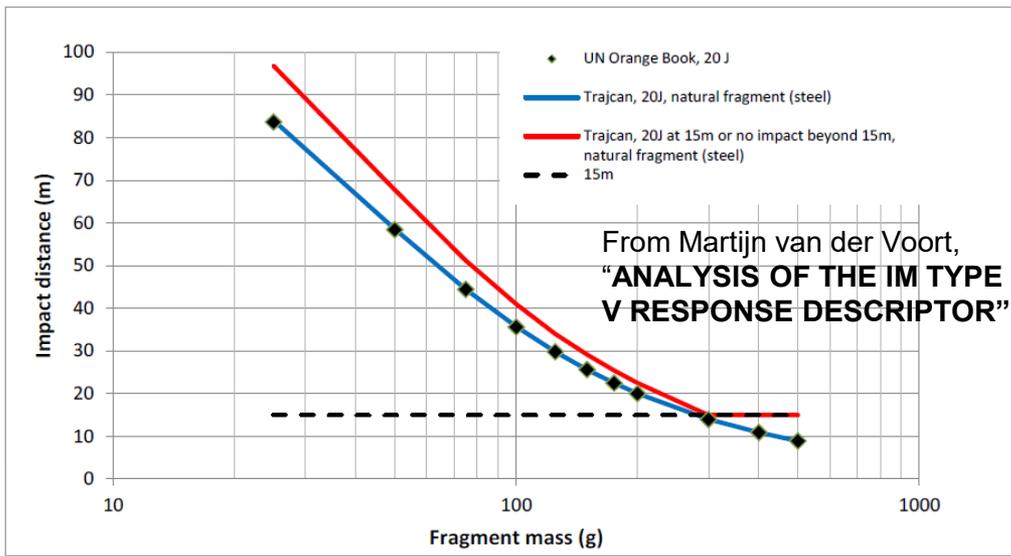
Perhaps orthogonal cameras or witness screens of some sort could provide angle/velocity cutoff information

-  New lower point used for impact mass-distance curve
-  Impacts Not Considered
-  Hazardous Impacts

If it can be photographically determined that the largest launch angle out of all the debris does not exceed a given value, the curve is lowered (fidelity of the measurement is gained)

Impact Energy at 15m (MSIAC Proposal) (Cont'd)

- MSIAC proposal is an **impact energy at 15m** criterion
 - This is different from an **impact energy** criterion (e.g., doesn't go off to infinity)
- Methodology
 - Find minimum possible launch velocity to hit person standing at 15m with a 20J impact
 - Using that velocity, adjust the launch angle until the maximum distance is found, this is the point used for their mass-distance curve
 - A fragment which lands above their curve has a higher velocity than the minimum velocity possible to reach a person standing at 15m with 20J
 - Therefore it **guarantees a person at 15m would be hit with at least 20J if the launch angle were lowered**



Pro: Guarantees hazardous impact at 15m if above curve, conservative lethality criterion reduces unknown region below curve

Con: Not much different from launch energy, lethality criterion may be too conservative